

24. (a) (i) [1996, 1998]:  $\frac{N(1998) - N(1996)}{1998 - 1996} = \frac{1886 - 1015}{2} = \frac{871}{2} = 435.5$  locations/year

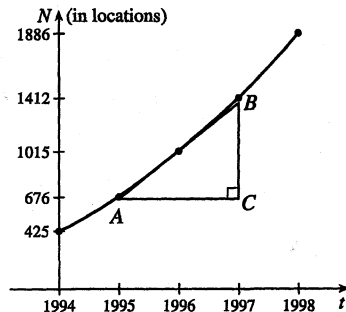
(ii) [1996, 1997]:  $\frac{N(1997) - N(1996)}{1997 - 1996} = \frac{1412 - 1015}{1} = 397$  locations/year

(iii) [1995, 1996]:  $\frac{N(1996) - N(1995)}{1996 - 1995} = \frac{1015 - 676}{1} = 339$  locations/year

(b) Using the values from (ii) and (iii), we have  $\frac{397 + 339}{2} = \frac{736}{2} = 368$  locations/year.

(c) Estimating  $A$  as (1995, 660) and  $B$  as (1997, 1350), the slope

at 1996 is  $\frac{1350 - 660}{1997 - 1995} = \frac{690}{2} = 345$  locations/year.



25. (a) (i)  $\frac{\Delta C}{\Delta x} = \frac{C(105) - C(100)}{105 - 100} = \frac{6601.25 - 6500}{5} = \$20.25/\text{unit}.$

(ii)  $\frac{\Delta C}{\Delta x} = \frac{C(101) - C(100)}{101 - 100} = \frac{6520.05 - 6500}{1} = \$20.05/\text{unit}.$

(b)  $\frac{C(100 + h) - C(100)}{h} = \frac{[5000 + 10(100 + h) + 0.05(100 + h)^2] - 6500}{h} = \frac{20h + 0.05h^2}{h}$   
 $= 20 + 0.05h, h \neq 0$

So the instantaneous rate of change is  $\lim_{h \rightarrow 0} \frac{C(100 + h) - C(100)}{h} = \lim_{h \rightarrow 0} (20 + 0.05h) = \$20/\text{unit}.$