

1.  $y = (x^4 - 3x^2 + 5)^3 \Rightarrow$   
 $y' = 3(x^4 - 3x^2 + 5)^2 \frac{d}{dx} (x^4 - 3x^2 + 5) = 3(x^4 - 3x^2 + 5)^2 (4x^3 - 6x) = 6x(x^4 - 3x^2 + 5)^2 (2x^2 - 3)$
2.  $y = \cos(\tan x) \Rightarrow y' = -\sin(\tan x) \frac{d}{dx} (\tan x) = -\sin(\tan x)(\sec^2 x)$
3.  $y = \sqrt{x} + \frac{1}{\sqrt[3]{x^4}} = x^{1/2} + x^{-4/3} \Rightarrow y' = \frac{1}{2}x^{-1/2} - \frac{4}{3}x^{-7/3} = \frac{1}{2\sqrt{x}} - \frac{4}{3\sqrt[3]{x^7}}$
10.  $y = \sin^{-1}(e^x) \Rightarrow y' = \frac{1}{\sqrt{1 - (e^x)^2}} \cdot e^x = e^x / \sqrt{1 - e^{2x}}$
11.  $y = xe^{-1/x} \Rightarrow y' = xe^{-1/x}(1/x^2) + e^{-1/x} \cdot 1 = e^{-1/x}(1/x + 1)$
12.  $y = x^r e^{sx} \Rightarrow y' = x^r (se^{sx}) + e^{sx} (rx^{r-1}) = e^{sx} x^{r-1} (sx + r)$
13.  $\frac{d}{dx} (xy^4 + x^2y) = \frac{d}{dx} (x + 3y) \Rightarrow x \cdot 4y^3y' + y^4 \cdot 1 + x^2 \cdot y' + y \cdot 2x = 1 + 3y' \Rightarrow$   
 $y'(4xy^3 + x^2 - 3) = 1 - y^4 - 2xy \Rightarrow y' = \frac{1 - y^4 - 2xy}{4xy^3 + x^2 - 3}$
14.  $y = \ln(\csc 5x) \Rightarrow y' = \frac{1}{\csc 5x} (-\csc 5x \cot 5x)(5) = -5 \cot 5x$
15.  $y = \frac{\sec 2\theta}{1 + \tan 2\theta} \Rightarrow$   
 $y' = \frac{(1 + \tan 2\theta)(\sec 2\theta \tan 2\theta \cdot 2) - (\sec 2\theta)(\sec^2 2\theta \cdot 2)}{(1 + \tan 2\theta)^2} = \frac{2 \sec 2\theta [(1 + \tan 2\theta) \tan 2\theta - \sec^2 2\theta]}{(1 + \tan 2\theta)^2}$   
 $= \frac{2 \sec 2\theta (\tan 2\theta + \tan^2 2\theta - \sec^2 2\theta)}{(1 + \tan 2\theta)^2} = \frac{2 \sec 2\theta (\tan 2\theta - 1)}{(1 + \tan 2\theta)^2} [1 + \tan^2 x = \sec^2 x]$
16.  $\frac{d}{dx} (x^2 \cos y + \sin 2y) = \frac{d}{dx} (xy) \Rightarrow x^2(-\sin y \cdot y') + (\cos y)(2x) + \cos 2y \cdot 2y' = x \cdot y' + y \cdot 1 \Rightarrow$   
 $y'(-x^2 \sin y + 2 \cos 2y - x) = y - 2x \cos y \Rightarrow y' = \frac{y - 2x \cos y}{2 \cos 2y - x^2 \sin y - x}$
17.  $y = e^{cx} (c \sin x - \cos x) \Rightarrow$   
 $y' = e^{cx} (c \cos x + \sin x) + ce^{cx} (c \sin x - \cos x)$   
 $= e^{cx} (c^2 \sin x - c \cos x + c \cos x + \sin x) = e^{cx} (c^2 \sin x + \sin x) = e^{cx} \sin x (c^2 + 1)$
18.  $y = \ln(x^2 e^x) = \ln x^2 + \ln e^x = 2 \ln x + x \Rightarrow y' = 2/x + 1$
24.  $y = e^{\cos x} + \cos(e^x) \Rightarrow y' = e^{\cos x} (-\sin x) + [-\sin(e^x) \cdot e^x] = -\sin x e^{\cos x} - e^x \sin(e^x)$