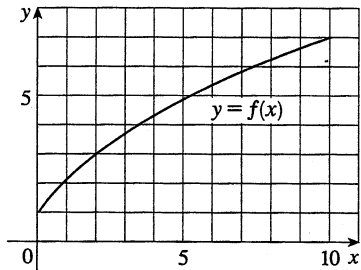


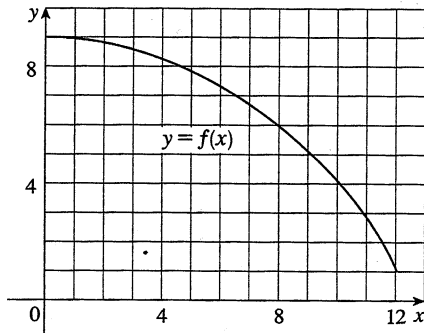
STEWART

5.1

1. (a) By reading values from the given graph of f , use five rectangles to find a lower estimate and an upper estimate for the area under the given graph of f from $x = 0$ to $x = 10$. In each case sketch the rectangles that you use.
 (b) Find new estimates using 10 rectangles in each case.



2. (a) Use six rectangles to find estimates of each type for the area under the given graph of f from $x = 0$ to $x = 12$.
 (i) L_6 (sample points are left endpoints)
 (ii) R_6 (sample points are right endpoints)
 (iii) M_6 (sample points are midpoints)
 (b) Is L_6 an underestimate or overestimate of the true area?
 (c) Is R_6 an underestimate or overestimate of the true area?



- (d) Which of the numbers L_6 , R_6 , or M_6 gives the best estimate? Explain.

3. (a) Estimate the area under the graph of $f(x) = 1/x$ from $x = 1$ to $x = 5$ using four approximating rectangles and right endpoints. Sketch the graph and the rectangles. Is your estimate an underestimate or an overestimate?
 (b) Repeat part (a) using left endpoints.
 4. (a) Estimate the area under the graph of $f(x) = 25 - x^2$ from $x = 0$ to $x = 5$ using five approximating rectangles and right endpoints. Sketch the graph and the rectangles. Is your estimate an underestimate or an overestimate?
 (b) Repeat part (a) using left endpoints.
 5. (a) Estimate the area under the graph of $f(x) = 1 + x^2$ from $x = -1$ to $x = 2$ using three rectangles and right endpoints. Then improve your estimate by using six rectangles. Sketch the curve and the approximating rectangles.
 (b) Repeat part (a) using left endpoints.
 (c) Repeat part (a) using midpoints.
 (d) From your sketches in parts (a), (b), and (c), which appears to be the best estimate?

11. The speed of a runner increased steadily during the first three seconds of a race. Her speed at half-second intervals is given in the table. Find lower and upper estimates for the distance that she traveled during these three seconds.

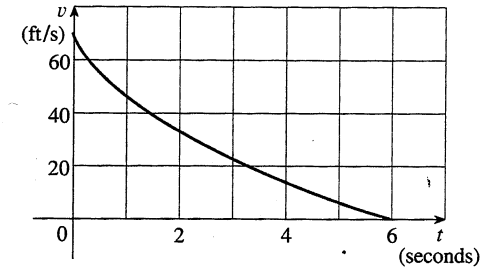
| | | | | | | | |
|------------|---|-----|------|------|------|------|------|
| t (s) | 0 | 0.5 | 1.0 | 1.5 | 2.0 | 2.5 | 3.0 |
| v (ft/s) | 0 | 6.2 | 10.8 | 14.9 | 18.1 | 19.4 | 20.2 |

12. When we estimate distances from velocity data it is sometimes necessary to use times $t_0, t_1, t_2, t_3, \dots$ that are not equally spaced. We can still estimate distances using the time periods $\Delta t_i = t_i - t_{i-1}$. For example, on May 7, 1992, the space shuttle *Endeavour* was launched on mission STS-49, the purpose of which was to install a new perigee kick motor in an Intelsat communications satellite. The table, provided by NASA, gives the velocity data for the shuttle between liftoff and the jettisoning of the solid rocket boosters.

| Event | Time (s) | Velocity (ft/s) |
|---------------------------------|----------|-----------------|
| Launch | 0 | 0 |
| Begin roll maneuver | 10 | 185 |
| End roll maneuver | 15 | 319 |
| Throttle to 89% | 20 | 447 |
| Throttle to 67% | 32 | 742 |
| Throttle to 104% | 59 | 1325 |
| Maximum dynamic pressure | 62 | 1445 |
| Solid rocket booster separation | 125 | 4151 |

Use these data to estimate the height above Earth's surface of the space shuttle *Endeavour*, 62 seconds after liftoff.

13. The velocity graph of a braking car is shown. Use it to estimate the distance traveled by the car while the brakes are applied.



14. The velocity graph of a car accelerating from rest to a speed of 120 km/h over a period of 30 seconds is shown. Estimate the distance traveled during this period.

