

6. $u = x, dv = \cos 2x dx, du = dx, v = \frac{1}{2} \sin 2x;$

$$\int x \cos 2x dx = \frac{1}{2} x \sin 2x - \frac{1}{2} \int \sin 2x dx = \frac{1}{2} x \sin 2x + \frac{1}{4} \cos 2x + C$$

7. $u = x^2, dv = \cos x dx, du = 2x dx, v = \sin x; \int x^2 \cos x dx = x^2 \sin x - 2 \int x \sin x dx$

For $\int x \sin x dx$ use $u = x, dv = \sin x dx$ to get

$$\int x \sin x dx = -x \cos x + \sin x + C_1 \text{ so } \int x^2 \cos x dx = x^2 \sin x + 2x \cos x - 2 \sin x + C$$

8. $u = x^2, dv = \sin x dx, du = 2x dx, v = -\cos x;$

$$\int x^2 \sin x dx = -x^2 \cos x + 2 \int x \cos x dx; \text{ for } \int x \cos x dx \text{ use } u = x, dv = \cos x dx \text{ to get}$$

$$\int x \cos x dx = x \sin x + \cos x + C_1 \text{ so } \int x^2 \sin x dx = -x^2 \cos x + 2x \sin x + 2 \cos x + C$$

9. $u = \ln x, dv = x dx, du = \frac{1}{x} dx, v = \frac{1}{2} x^2; \int x \ln x dx = \frac{1}{2} x^2 \ln x - \frac{1}{2} \int x dx = \frac{1}{2} x^2 \ln x - \frac{1}{4} x^2 + C$

10. $u = \ln x, dv = \sqrt{x} dx, du = \frac{1}{x} dx, v = \frac{2}{3} x^{3/2};$

$$\int \sqrt{x} \ln x dx = \frac{2}{3} x^{3/2} \ln x - \frac{2}{3} \int x^{1/2} dx = \frac{2}{3} x^{3/2} \ln x - \frac{4}{9} x^{3/2} + C$$

11. $u = (\ln x)^2, dv = dx, du = 2 \frac{\ln x}{x} dx, v = x; \int (\ln x)^2 dx = x(\ln x)^2 - 2 \int \ln x dx.$

Use $u = \ln x, dv = dx$ to get $\int \ln x dx = x \ln x - \int dx = x \ln x - x + C_1$ so

$$\int (\ln x)^2 dx = x(\ln x)^2 - 2x \ln x + 2x + C$$

12. $u = \ln x, dv = \frac{1}{\sqrt{x}} dx, du = \frac{1}{x} dx, v = 2\sqrt{x}; \int \frac{\ln x}{\sqrt{x}} dx = 2\sqrt{x} \ln x - 2 \int \frac{1}{\sqrt{x}} dx = 2\sqrt{x} \ln x - 4\sqrt{x} + C$

13. $u = \ln(3x - 2), dv = dx, du = \frac{3}{3x - 2} dx, v = x; \int \ln(3x - 2) dx = x \ln(3x - 2) - \int \frac{3x}{3x - 2} dx$

but $\int \frac{3x}{3x - 2} dx = \int \left(1 + \frac{2}{3x - 2}\right) dx = x + \frac{2}{3} \ln(3x - 2) + C_1$ so

$$\int \ln(3x - 2) dx = x \ln(3x - 2) - x - \frac{2}{3} \ln(3x - 2) + C$$

14. $u = \ln(x^2 + 4), dv = dx, du = \frac{2x}{x^2 + 4} dx, v = x; \int \ln(x^2 + 4) dx = x \ln(x^2 + 4) - 2 \int \frac{x^2}{x^2 + 4} dx$

but $\int \frac{x^2}{x^2 + 4} dx = \int \left(1 - \frac{4}{x^2 + 4}\right) dx = x - 2 \tan^{-1} \frac{x}{2} + C_1$ so

$$\int \ln(x^2 + 4) dx = x \ln(x^2 + 4) - 2x + 4 \tan^{-1} \frac{x}{2} + C$$