

15.  $u = \sin^{-1} x$ ,  $dv = dx$ ,  $du = 1/\sqrt{1-x^2}dx$ ,  $v = x$ ;

$$\int \sin^{-1} x dx = x \sin^{-1} x - \int x/\sqrt{1-x^2}dx = x \sin^{-1} x + \sqrt{1-x^2} + C$$

16.  $u = \cos^{-1}(2x)$ ,  $dv = dx$ ,  $du = -\frac{2}{\sqrt{1-4x^2}}dx$ ,  $v = x$ ;

$$\int \cos^{-1}(2x)dx = x \cos^{-1}(2x) + \int \frac{2x}{\sqrt{1-4x^2}}dx = x \cos^{-1}(2x) - \frac{1}{2}\sqrt{1-4x^2} + C$$

17.  $u = \tan^{-1}(3x)$ ,  $dv = dx$ ,  $du = \frac{3}{1+9x^2}dx$ ,  $v = x$ ;

$$\int \tan^{-1}(3x)dx = x \tan^{-1}(3x) - \int \frac{3x}{1+9x^2}dx = x \tan^{-1}(3x) - \frac{1}{6}\ln(1+9x^2) + C$$

18.  $u = \tan^{-1} x$ ,  $dv = x dx$ ,  $du = \frac{1}{1+x^2}dx$ ,  $v = \frac{1}{2}x^2$ ;  $\int x \tan^{-1} x dx = \frac{1}{2}x^2 \tan^{-1} x - \frac{1}{2} \int \frac{x^2}{1+x^2}dx$

but  $\int \frac{x^2}{1+x^2}dx = \int \left(1 - \frac{1}{1+x^2}\right)dx = x - \tan^{-1} x + C_1$  so

$$\int x \tan^{-1} x dx = \frac{1}{2}x^2 \tan^{-1} x - \frac{1}{2}x + \frac{1}{2}\tan^{-1} x + C$$