

$$49. \quad \frac{dI}{dt} + \frac{R}{L}I = \frac{V(t)}{L}, \mu = e^{(R/L)\int dt} = e^{Rt/L}, \frac{d}{dt}(e^{Rt/L}I) = \frac{V(t)}{L}e^{Rt/L},$$

$$Ie^{Rt/L} = I(0) + \frac{1}{L} \int_0^t V(u)e^{Ru/L} du, I(t) = I(0)e^{-Rt/L} + \frac{1}{L}e^{-Rt/L} \int_0^t V(u)e^{Ru/L} du.$$

$$(a) \quad I(t) = \frac{1}{5}e^{-2t} \int_0^t 20e^{2u} du = 2e^{-2t} e^{2u} \Big|_0^t = 2(1 - e^{-2t}) \text{ A.}$$

$$(b) \quad \lim_{t \rightarrow +\infty} I(t) = 2 \text{ A}$$

$$55. \quad \frac{dv}{dt} = -\frac{1}{32}v^2, \frac{1}{v^2}dv = -\frac{1}{32}dt, -\frac{1}{v} = -\frac{1}{32}t + C; v = 128 \text{ when } t = 0 \text{ so } -\frac{1}{128} = C,$$

$$-\frac{1}{v} = -\frac{1}{32}t - \frac{1}{128}, v = \frac{128}{4t+1} \text{ cm/s. But } v = \frac{dx}{dt} \text{ so } \frac{dx}{dt} = \frac{128}{4t+1}, x = 32 \ln(4t+1) + C_1;$$

$$x = 0 \text{ when } t = 0 \text{ so } C_1 = 0, x = 32 \ln(4t+1) \text{ cm.}$$

$$56. \quad \frac{dv}{dt} = -0.02\sqrt{v}, \frac{1}{\sqrt{v}}dv = -0.02dt, 2\sqrt{v} = -0.02t + C; v = 9 \text{ when } t = 0 \text{ so } 6 = C,$$

$$2\sqrt{v} = -0.02t + 6, v = (3 - 0.01t)^2 \text{ cm/s. But } v = \frac{dx}{dt} \text{ so } \frac{dx}{dt} = (3 - 0.01t)^2,$$

$$x = -\frac{100}{3}(3 - 0.01t)^3 + C_1; x = 0 \text{ when } t = 0 \text{ so } C_1 = 900, x = 900 - \frac{100}{3}(3 - 0.01t)^3 \text{ cm.}$$