

$$6. \int_2^{\infty} \frac{dx}{(x+3)^{3/2}} = \lim_{t \rightarrow \infty} \int_2^t \frac{dx}{(x+3)^{3/2}} = \lim_{t \rightarrow \infty} \left[\frac{-2}{\sqrt{x+3}} \right]_2^t = \lim_{t \rightarrow \infty} \left[\frac{-2}{\sqrt{t+3}} + \frac{2}{\sqrt{5}} \right] = \frac{2}{\sqrt{5}}. \text{ Convergent}$$

$$7. \int_0^{\infty} e^{-x} dx = \lim_{t \rightarrow \infty} \int_0^t e^{-x} dx = \lim_{t \rightarrow \infty} [-e^{-x}]_0^t = \lim_{t \rightarrow \infty} (-e^{-t} + 1) = 1. \text{ Convergent}$$

$$8. \int_{-\infty}^0 \frac{1}{2x-5} dx = \lim_{t \rightarrow -\infty} \int_t^0 \frac{1}{2x-5} dx = \lim_{t \rightarrow -\infty} \left[\frac{1}{2} \ln |2x-5| \right]_t^0 = \lim_{t \rightarrow -\infty} \left[\frac{1}{2} \ln 5 - \frac{1}{2} \ln |2t-5| \right] = -\infty.$$

Divergent

$$9. \int_{-\infty}^{-1} \frac{1}{\sqrt{2-w}} dw = \lim_{t \rightarrow -\infty} \int_t^{-1} \frac{1}{\sqrt{2-w}} dw = \lim_{t \rightarrow -\infty} [-2\sqrt{2-w}]_t^{-1} \quad [u = 2-w, du = -dw]$$

$$= \lim_{t \rightarrow -\infty} [-2\sqrt{3} + 2\sqrt{2-t}] = \infty. \text{ Divergent}$$

$$10. \int_{-\infty}^{-1} e^{-2t} dt = \lim_{x \rightarrow -\infty} \int_x^{-1} e^{-2t} dt = \lim_{x \rightarrow -\infty} \left[-\frac{1}{2} e^{-2t} \right]_x^{-1} = \lim_{x \rightarrow -\infty} \left[-\frac{1}{2} e^2 + \frac{1}{2} e^{-2x} \right] = \infty. \text{ Divergent}$$

$$11. I = \int_{-\infty}^{\infty} x^3 dx = I_1 + I_2 = \int_{-\infty}^0 x^3 dx + \int_0^{\infty} x^3 dx, \text{ but } I_1 = \lim_{t \rightarrow -\infty} \left[\frac{1}{4} x^4 \right]_t^0 = \lim_{t \rightarrow -\infty} \left(-\frac{1}{4} t^4 \right) = -\infty. \text{ Since } I_1$$

is divergent, I is divergent, and there is no need to evaluate I_2 . Divergent

$$12. I = \int_{-\infty}^{\infty} (2 - v^4) dv = I_1 + I_2 = \int_{-\infty}^0 (2 - v^4) dv + \int_0^{\infty} (2 - v^4) dv, \text{ but}$$

$$I_1 = \lim_{t \rightarrow -\infty} \left[2v - \frac{1}{5} v^5 \right]_t^0 = \lim_{t \rightarrow -\infty} \left(-2t + \frac{1}{5} t^5 \right) = -\infty. \text{ Since } I_1 \text{ is divergent, } I \text{ is divergent, and there is no need}$$

to evaluate I_2 . Divergent

$$13. \int_{-\infty}^{\infty} x e^{-x^2} dx = \int_{-\infty}^0 x e^{-x^2} dx + \int_0^{\infty} x e^{-x^2} dx.$$

$$\int_{-\infty}^0 x e^{-x^2} dx = \lim_{t \rightarrow -\infty} \left(-\frac{1}{2} \right) \left[e^{-x^2} \right]_t^0 = \lim_{t \rightarrow -\infty} \left(-\frac{1}{2} \right) (1 - e^{-t^2}) = -\frac{1}{2} \cdot 1 = -\frac{1}{2}, \text{ and}$$

$$\int_0^{\infty} x e^{-x^2} dx = \lim_{t \rightarrow \infty} \left(-\frac{1}{2} \right) \left[e^{-x^2} \right]_0^t = \lim_{t \rightarrow \infty} \left(-\frac{1}{2} \right) (e^{-t^2} - 1) = -\frac{1}{2} \cdot (-1) = \frac{1}{2}.$$

$$\text{Therefore, } \int_{-\infty}^{\infty} x e^{-x^2} dx = -\frac{1}{2} + \frac{1}{2} = 0. \text{ Convergent}$$

$$14. \int_{-\infty}^{\infty} x^2 e^{-x^3} dx = \int_{-\infty}^0 x^2 e^{-x^3} dx + \int_0^{\infty} x^2 e^{-x^3} dx, \text{ and}$$

$$\int_{-\infty}^0 x^2 e^{-x^3} dx = \lim_{t \rightarrow -\infty} \left[-\frac{1}{3} e^{-x^3} \right]_t^0 = -\frac{1}{3} + \frac{1}{3} \left(\lim_{t \rightarrow -\infty} e^{-t^3} \right) = \infty. \text{ Divergent}$$