

30. $\sin x - 2 \sin^2 x = 0 \Leftrightarrow \sin x (1 - 2 \sin x) = 0 \Leftrightarrow \sin x = 0$ or $\sin x = \frac{1}{2} \Leftrightarrow x = 0, \pi$
 or $x = \frac{\pi}{6}, \frac{5\pi}{6}$. Therefore, the solutions in $[0, 2\pi)$ are $x = 0, \frac{\pi}{6}, \frac{5\pi}{6}, \pi$.

32. $\sin x - \cos x - \tan x = -1 \Leftrightarrow \sin x \cos x - \cos^2 x - \sin x = -\cos x \Leftrightarrow$
 $\sin x \cos x - \sin x - \cos^2 x + \cos x = 0 \Leftrightarrow \sin x (\cos x - 1) - \cos x (\cos x - 1) = 0 \Leftrightarrow$
 $(\sin x - \cos x)(\cos x - 1) = 0 \Leftrightarrow \sin x = \cos x$ or $\cos x = 1 \Leftrightarrow \tan x = 1$ or $\cos x = 1$
 $\Leftrightarrow x = \frac{\pi}{4}, \frac{5\pi}{4}$ or $x = 0$. Therefore, the solutions in $[0, 2\pi)$ are $x = 0, \frac{\pi}{4}, \frac{5\pi}{4}$.

34. $4 \sin^2 x + 2 \cos^2 x = 3 \Leftrightarrow 2 \sin^2 x + 2 (\sin^2 x + \cos^2 x) - 3 = 0 \Leftrightarrow 2 \sin^2 x + 2 - 3 = 0$
 $\Leftrightarrow 2 \sin^2 x = 1 \Leftrightarrow \sin x = \pm \frac{1}{\sqrt{2}}$. So the solution in $[0, 2\pi)$ are $x = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$.

36. $\sin x = \cos 2x \Leftrightarrow \sin x = 1 - 2 \sin^2 x \Leftrightarrow 2 \sin^2 x + \sin x - 1 = 0 \Leftrightarrow$
 $(2 \sin x - 1)(\sin x + 1) = 0 \Leftrightarrow \sin x = \frac{1}{2}$ or $\sin x = -1 \Leftrightarrow x = \frac{\pi}{6}, \frac{5\pi}{6}$ or $x = \frac{3\pi}{2}$. Thus,
 the solutions in $[0, 2\pi)$ are $x = \frac{\pi}{6}, \frac{3\pi}{2}, \frac{5\pi}{6}$.