- 2. $\begin{cases} 2x + y = 7 \\ 3x y = 13 \end{cases}$ Solving the first equation for y, we get y = 7 2x and substituting this into the second equation, gives $2x + (7 2x) = 13 \Leftrightarrow 5x = 20 \Leftrightarrow x = 4$. Substituting for x we get y = 7 2x = 7 2(4) = -1. Thus the solution is (4, -1).
- 4. $\begin{cases} x^2 + y^2 = 25 \\ y = \frac{3}{4}x \end{cases}$ Substituting for y in the first equation gives $x^2 + \left(\frac{3}{4}x\right)^2 = 25 \Leftrightarrow \frac{25}{16}x^2 = 25$ $\Leftrightarrow x^2 = 16 \Rightarrow x = \pm 4. \text{ When } x = 4 \text{ then } y = \frac{3}{4}(4) = 3, \text{ and when } x = -4 \text{ then } y = \frac{3}{4}(-4) = -3. \text{ Thus the solutions are } (4,3) \text{ and } (-4,-3).$
- 6. $\begin{cases} x^2+y=9 \\ x-y+3=0 \end{cases}$ Solving the first equation for y, we get $y=9-x^2$. Substituting this into the second equation gives $x-(9-x^2)+3=0 \Leftrightarrow x^2+x-6=0 \Leftrightarrow (x+3)(x-2)=0 \Leftrightarrow x=-3 \text{ or } x=2.$ If x=-3, then $y=9-(-3)^2=0$, and if x=2, then $y=9-(2)^2=5$. Thus the solutions are (-3,0) and (2,5).
- 8. $\begin{cases} 4x 3y = 10 \\ 9x + 4y = 1 \end{cases}$ Multiplying the first equation by 4 and the second by 3 gives the system $\begin{cases} 16x 12y = 40 \\ 27x + 12y = 3 \end{cases}$ Adding, we get $43x = 43 \Leftrightarrow x = 1$. Substituting this value into the second equation gives $9(1) + 4y = 1 \Leftrightarrow 4y = -8 \Leftrightarrow y = -2$. Thus the solution is (1, -2).
- 10. $\begin{cases} 3x^2 + 4y = 17 \\ 2x^2 + 5y = 2 \end{cases}$ Multiplying the first equation by 2 and the second by 3 gives the system $\begin{cases} 6x^2 + 8y = 34 \\ -6x^2 15y = -6 \end{cases}$ Adding we get $-7y = 28 \implies y = -4$. Substituting this value into the second equation gives $2x^2 + 5(-4) = 2 \implies 2x^2 = 22 \implies x^2 = 11 \implies x = \pm \sqrt{11}$. Thus the solutions are $(\sqrt{11}, -4)$ and $(-\sqrt{11}, -4)$.
- 14. $\begin{cases} x-y^2=0 \\ y-x^2=0 \end{cases}$ Solving the first equation for x and the second equation for y gives $\begin{cases} x=y^2 \\ y=x^2 \end{cases}$ Substituting for y in the first equation gives $x=x^4 \Leftrightarrow x(x^3-1)=0 \Leftrightarrow x=0, x=1$. Thus, the solutions are (0,0) and (1,1).