- 17.  $\begin{cases} 2x 6y = 10 \\ -3x + 9y = -15 \end{cases}$  Adding 3 times the first equation to 2 times the second equation gives
  - -6x + 18y = -30 $\overline{0=0}$ . Writing the equation in slope-intercept form, we have 2x-6y=10  $\Leftrightarrow$  $\Leftrightarrow y = \frac{1}{3}x - \frac{5}{3}$ , so a solution is any pair of the form  $(x, \frac{1}{3}x - \frac{5}{3})$ , where x is -6y = -2x + 10
- 19.  $\begin{cases} 6x + 4y = 12 \\ 9x + 6y = 18 \end{cases}$  Adding 3 times the first equation to -2 times the second equation gives

any real number.

- 18x + 12y = 36
- -18x 12y = -360=0 . Writing the equation in slope-intercept form, we have 6x+4y=12
- 4y = -6x + 12  $\Leftrightarrow$   $y = -\frac{3}{2}x + 3$ , so a solution is any pair of the form  $\left(x, -\frac{3}{2}x + 3\right)$ , where xis any real number.
- 21.  $\begin{cases} 8s 3t = -3 \\ 5s 2t = -1 \end{cases}$  Adding 2 times the first equation to 3 times the second equation gives  $\frac{15s - 6t = -3}{s = -3}$  So 8(-3) - 3t = -3  $\Leftrightarrow$  -24 - 3t = -3  $\Leftrightarrow$  t = -7. Thus, the solution is (s, t) = (-3, -7).
- 23.  $\begin{cases} \frac{1}{2}x + \frac{3}{5}y = 3\\ \frac{5}{3}x + 2y = 10 \end{cases}$  Adding 10 times the first equation to -3 times the second equation gives 5x + 6y = 30 $\frac{-5x - 6y = -30}{0 = 0}$ . Writing the equation in slope-intercept form, we have  $\frac{1}{2}x + \frac{3}{5}y = 3 \Leftrightarrow \frac{3}{5}x + \frac{3}{5}y = 3$   $\Leftrightarrow$
- $\frac{3}{5}y = -\frac{1}{2}x + 3 \Leftrightarrow y = -\frac{5}{6}x + 5$ , so a solution is any pair of the form  $\left(x, -\frac{5}{6}x + 5\right)$ , where x is any real number. 25.  $\begin{cases} \frac{2x-5}{3} + \frac{y-1}{6} = \frac{1}{2} \\ \frac{x}{5} + \frac{3y-6}{12} = 1 \end{cases}$ . We multiply the first equation by 6 and the second equation by 60 gives
  - the system  $\begin{cases} 4x-10+y-1=3\\ 12x+15y-30=60 \end{cases}$ , which simplifies to  $\begin{cases} 4x+y=14\\ 12x+15y=90 \end{cases}$  Then adding 3 times the first equation to -1 times the second equation gives
  - $\frac{-12x 15y = -90}{-12y = -48} \quad \Leftrightarrow \quad y = 4.$
- So 4x + (4) = 14  $\Leftrightarrow$  4x = 10  $\Leftrightarrow$   $x = \frac{5}{2}$ . Thus, the solution is  $(\frac{5}{2}, 4)$ . x - 2y = 127.
  - $\begin{array}{ccc}
    2x + 2y &= 1 \\
    3x &= 2 & \Leftrightarrow & x &= \frac{2}{3}.
    \end{array}$ So  $\left(\frac{2}{3}\right) - 2y = 1$   $\Leftrightarrow$   $2y = -\frac{1}{3}$   $\Leftrightarrow$   $y = -\frac{1}{6}$ . Thus the solution is  $\left(\frac{2}{3}, -\frac{1}{6}\right)$ .