

52. Using  $h = -1$ ,  $k = -4$ , and  $r = 8$  we get  $(x - (-1))^2 + (y - (-4))^2 = 8^2 \Leftrightarrow (x + 1)^2 + (y + 4)^2 = 64$ .
54. Using  $h = -1$  and  $k = 5$  we get  $(x - (-1))^2 + (y - 5)^2 = r^2 \Leftrightarrow (x + 1)^2 + (y - 5)^2 = r^2$ . Next, using the point  $(-4, -6)$ , we solve for  $r^2$ . This gives  $(-4 + 1)^2 + (-6 - 5)^2 = r^2 \Leftrightarrow 130 = r^2$ . Thus, the equation of the circle is  $(x + 1)^2 + (y - 5)^2 = 130$ .
56. The center is at the midpoint of the line segment, which is  $(\frac{-1+7}{2}, \frac{3+(-5)}{2}) = (3, -1)$ . The radius is one half the diameter, so  $r = \frac{1}{2}\sqrt{(-1 - 7)^2 + (3 - (-5))^2} = 4\sqrt{2}$ . Thus, the equation of the circle is  $(x - 3)^2 + (y + 1)^2 = 32$ .
58. Since the circle with  $r = 5$  lies in the first quadrant and is tangent to both the  $x$ -axis and the  $y$ -axis, the center of the circle is at  $(5, 5)$ . Therefore, the equation of the circle is  $(x - 5)^2 + (y - 5)^2 = 25$ .
60. From the figure, the center of the circle is at  $(-1, 1)$ . The radius is the distance from the center to the point  $(2, 0)$ . Thus  $r = \sqrt{(-1 - 2)^2 + (1 - 0)^2} = \sqrt{9 + 1} = \sqrt{10}$ , and the equation of the circle is  $(x + 1)^2 + (y - 1)^2 = 10$ .