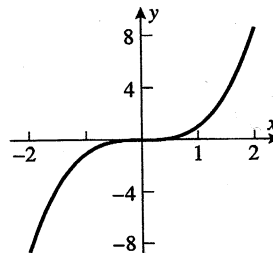


1. (a)  $f(g(x)) = 4(x/4) = x$ ,  $g(f(x)) = (4x)/4 = x$ ,  $f$  and  $g$  are inverse functions  
 (b)  $f(g(x)) = 3(3x - 1) + 1 = 9x - 2 \neq x$  so  $f$  and  $g$  are not inverse functions  
 (c)  $f(g(x)) = \sqrt[3]{(x^3 + 2) - 2} = x$ ,  $g(f(x)) = (x - 2) + 2 = x$ ,  $f$  and  $g$  are inverse functions  
 (d)  $f(g(x)) = (x^{1/4})^4 = x$ ,  $g(f(x)) = (x^4)^{1/4} = |x| \neq x$ ,  $f$  and  $g$  are not inverse functions

5. (a) yes; all outputs (the elements of row two) are distinct  
 (b) no;  $f(1) = f(6)$

7. (a)  $f$  has an inverse because the graph passes the horizontal line test. To compute  $f^{-1}(2)$  start at 2 on the  $y$ -axis and go to the curve and then down, so  $f^{-1}(2) = 8$ ; similarly,  $f^{-1}(-1) = -1$  and  $f^{-1}(0) = 0$ .

- (b) domain of  $f^{-1}$  is  $[-2, 2]$ , range is  $[-8, 8]$  (c)



8. (a) the horizontal line test fails  
 (b)  $-3 < x \leq -1$ ;  $-1 \leq x \leq 2$ ; and  $2 \leq x < 4$ .

24. (a)  $C = \frac{5}{9}(F - 32)$

- (b) how many degrees Celsius given the Fahrenheit temperature

- (c)  $C = -273.15^\circ \text{C}$  is equivalent to  $F = -459.67^\circ \text{F}$ , so the domain is  $F \geq -459.67$ , the range is  $C \geq -273.15$

27. (a)  $f(f(x)) = \frac{3 - \frac{3-x}{1-x}}{1 - \frac{3-x}{1-x}} = \frac{3 - 3x - 3 + x}{1 - x - 3 + x} = x$  so  $f = f^{-1}$

- (b) symmetric about the line  $y = x$

29. if  $f^{-1}(x) = 1$ , then  $x = f(1) = 2(1)^3 + 5(1) + 3 = 10$

30. if  $f^{-1}(x) = 2$ , then  $x = f(2) = (2)^3 / [(2)^2 + 1] = 8/5$