

72. (a)  $f(x) = \ln(\ln(\ln x))$ . We must have  $\ln(\ln x) > 0 \Leftrightarrow \ln x > 1 \Leftrightarrow x > e$ . So the domain of  $f$  is  $(e, \infty)$ .
- (b)  $y = \ln(\ln(\ln x)) \Leftrightarrow e^y = \ln(\ln x) \Leftrightarrow e^{e^y} = \ln x \Leftrightarrow e^{e^{e^y}} = x$ . Thus the inverse function is  $f^{-1}(x) = e^{e^{e^x}}$ .
74. (a) Since 2 feet = 24 inches, the height of the graph is  $2^{24} = 1677216$  inches. Now, since there are 12 inches per foot and 5280 feet per mile, there are  $12(5280) = 63360$  inches per mile. So the height of the graph is  $\frac{1677216}{63360} \approx 264.8$ , or about 265 miles.
- (b) Since  $\log_2(2^{24}) = 24$ , we must be about  $2^{24}$  inches  $\approx 265$  miles to the right of the origin before the height of the graph of  $y = \log_2 x$  reaches 24 inches or 2 feet.
76. Notice that  $\log_a x$  is increasing for  $a > 1$ . So we have  $\log_4 17 > \log_4 16 = \log_4 4^2 = 2$ . Also, we have  $\log_5 24 < \log_5 25 = \log_5 5^2 = 2$ . Thus,  $\log_5 24 < 2 < \log_4 17$ .