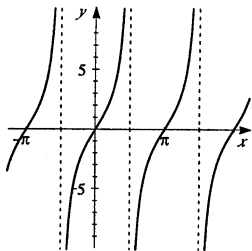
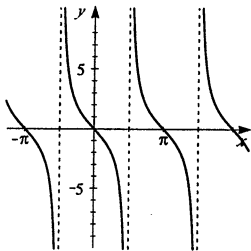


39. From the graph we see that the amplitude is $\frac{1}{2}$, the period is 1, and there is a phase shift of $-\frac{1}{3}$. Therefore, the function is $y = \frac{1}{2} \sin 2\pi(x + \frac{1}{3})$.

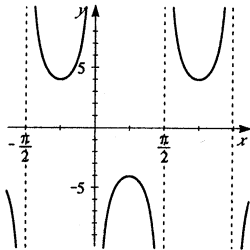
41. $y = 3 \tan x$, period = π



43. $y = 2 \cot(x - \frac{\pi}{2})$, period = π



45. $y = 4 \csc(2x - \pi) = 4 \csc 2(x - \frac{\pi}{2})$,
period = $\frac{2\pi}{2} = \pi$



47. $y = \tan(\frac{1}{2}x - \frac{\pi}{8}) = \tan \frac{1}{2}(x - \frac{\pi}{4})$,
period = $\frac{\pi}{(\frac{1}{2})} = 2\pi$

