

$$35. \log x = -2 \Leftrightarrow x = 10^{-2} = 0.01$$

$$37. \log(3x + 5) = 2 \Leftrightarrow 3x + 5 = 10^2 = 100 \Leftrightarrow 3x = 95 \Leftrightarrow x = \frac{95}{3} \approx 31.6667$$

$$39. 2 - \ln(3 - x) = 0 \Leftrightarrow 2 = \ln(3 - x) \Leftrightarrow e^2 = 3 - x \Leftrightarrow x = 3 - e^2 \approx -4.3891$$

$$41. \log_2 3 + \log_2 x = \log_2 5 + \log_2(x - 2) \Leftrightarrow \log_2(3x) = \log_2(5x - 10) \Leftrightarrow 3x = 5x - 10 \\ \Leftrightarrow 2x = 10 \Leftrightarrow x = 5$$

$$43. \log x + \log(x - 1) = \log(4x) \Leftrightarrow \log[x(x - 1)] = \log(4x) \Leftrightarrow x^2 - x = 4x \Leftrightarrow \\ x^2 - 5x = 0 \Leftrightarrow x(x - 5) = 0 \Rightarrow x = 0 \text{ or } x = 5. \text{ So the possible solutions are } x = 0 \text{ and } \\ x = 5. \text{ However, when } x = 0, \log x \text{ is undefined. Thus the only solution is } x = 5.$$

$$45. \log_5(x + 1) - \log_5(x - 1) = 2 \Leftrightarrow \log_5\left(\frac{x + 1}{x - 1}\right) = 2 \Leftrightarrow \frac{x + 1}{x - 1} = 5^2 \Leftrightarrow \\ x + 1 = 25x - 25 \Leftrightarrow 24x = 26 \Leftrightarrow x = \frac{13}{12}$$

$$47. \log_9(x - 5) + \log_9(x + 3) = 1 \Leftrightarrow \log_9[(x - 5)(x + 3)] = 1 \Leftrightarrow (x - 5)(x + 3) = 9^1 \\ \Leftrightarrow x^2 - 2x - 24 = 0 \Leftrightarrow (x - 6)(x + 4) = 0 \Rightarrow x = 6 \text{ or } -4. \text{ However, } x = -4 \text{ is } \\ \text{inadmissible, so } x = 6 \text{ is the only solution.}$$