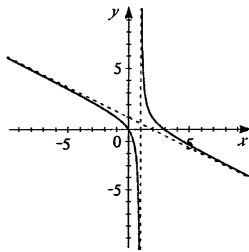
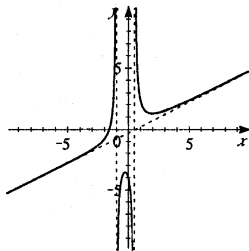


50. $r(x) = \frac{3x - x^2}{2x - 2} = \frac{x(3 - x)}{2(x - 1)}$. When $x = 0$, we have $y = 0$, so the graph passes through the origin. Also, when $y = 0$, we have $x = 0$ or $x = 3$, so the x -intercepts are 0 and 3. The vertical asymptote is $x = 1$. There is no horizontal asymptote, and the line $y = -\frac{1}{2}x + 1$ is a slant asymptote because by long division we have $y = -\frac{1}{2}x + 1 + \frac{1}{x - 1}$.



52. $r(x) = \frac{x^3 + 4}{2x^2 + x - 1} = \frac{x^3 + 4}{(2x - 1)(x + 1)}$. When $x = 0$, we have $y = \frac{0+4}{0+0-1} = -4$, so the y -intercept is -4 . Since $x^3 + 4 = 0 \Rightarrow x = -\sqrt[3]{4}$, the x -intercept is $x = -\sqrt[3]{4}$. There are vertical asymptotes where $(2x - 1)(x + 1) = 0 \Rightarrow x = \frac{1}{2}$ or $x = -1$. Since the degree of the numerator is greater than the degree of the denominator, there is no horizontal asymptote. By long division, we have $y = \frac{1}{2}x - \frac{1}{4} + \frac{\frac{3}{4}x + \frac{15}{4}}{2x^2 - x - 1}$, so the line $y = \frac{1}{2}x - \frac{1}{4}$ is a slant asymptote.



54. $r(x) = \frac{2x^3 + 2x}{x^2 - 1} = \frac{2x(x^2 + 1)}{(x - 1)(x + 1)}$. When $x = 0$, we have $y = 0$, so the graph passes through the origin. Also, note that $x^2 + 1 > 0$, for all real x , so the only x -intercept is 0. There are two vertical asymptotes at $x = -1$ and $x = 1$. There is no horizontal asymptote, and the line $y = 2x$ is a slant asymptote because by long division, we have $y = 2x + \frac{4x}{x^2 - 1}$.

