

50. (a) $s = r\theta \Leftrightarrow \theta = \frac{s}{r} = \frac{6155}{3960} \approx 1.5543 \text{ rad} \approx 89.05^\circ$

(b) Let d represent the distance, in miles, from the center of the earth to the moon. Since $\cos \theta = \frac{3960}{d}$, we have $d = \frac{3960}{\cos \theta} \approx \frac{3960}{\cos 89.05^\circ} \approx 239,961.5$. So the distance AC is $239,961.5 - 3960 \approx 236,000$ mi.

52. Let d represent the distance, in miles, from the earth to Alpha Centauri. Since $\sin 0.000211^\circ = \frac{93,000,000}{d}$, we have $d = \frac{93,000,000}{\sin 0.000211^\circ} \approx 25,253,590,022,410$. So the distance from the earth to Alpha Centauri is about 2.53×10^{13} mi.

54. Let d be the length of the base of the 60° triangle. Then $\tan 60^\circ = \frac{85}{d} \Leftrightarrow$
 $d = \frac{85}{\tan 60^\circ} \approx 49.075$, and so $\tan 30^\circ = \frac{85}{d+x} \Leftrightarrow d+x = \frac{85}{\tan 30^\circ} \Leftrightarrow$
 $x = \frac{85}{\tan 30^\circ} - d \approx 98.1$.

56. Let h be the hypotenuse of the top triangle. Then $\sin 30^\circ = \frac{5}{h} \Leftrightarrow h = \frac{5}{\sin 30^\circ} = 10$, and so
 $\tan 60^\circ = \frac{h}{x} \Leftrightarrow x = \frac{h}{\tan 60^\circ} = \frac{10}{\tan 60^\circ} \approx 5.8$.