

59.  $\sin t = \frac{3}{5}$  and  $t$  is in quadrant II, so the terminal point determined by  $t$  is  $P(x, \frac{3}{5})$ . Since  $P$  is on the unit circle  $x^2 + (\frac{3}{5})^2 = 1$ . Solving for  $x$  gives  $x = \pm\sqrt{1 - \frac{9}{25}} = \pm\sqrt{\frac{16}{25}} = \pm\frac{4}{5}$ . Since  $t$  is in quadrant III,  $x = -\frac{4}{5}$ . Thus the terminal point is  $P(-\frac{4}{5}, \frac{3}{5})$ . Thus,  $\cos t = -\frac{4}{5}$ ,  $\tan t = -\frac{3}{4}$ ,  $\csc t = \frac{5}{3}$ ,  $\sec t = -\frac{5}{4}$ ,  $\cot t = -\frac{4}{3}$ .
61.  $\tan t = -\frac{3}{4}$  and  $\cos t > 0$ , so  $t$  is in quadrant IV. Since  $\sec^2 t = \tan^2 t + 1$  we have  $\sec^2 t = (-\frac{3}{4})^2 + 1 = \frac{9}{16} + 1 = \frac{25}{16}$ . Thus  $\sec t = \pm\sqrt{\frac{25}{16}} = \pm\frac{5}{4}$ . Since  $\cos t > 0$ , we have  $\cos t = \frac{1}{\sec t} = \frac{1}{\frac{5}{4}} = \frac{4}{5}$ . Let  $P(\frac{4}{5}, y)$ . Since  $\tan t \cdot \cos t = \sin t$  we have  $\sin t = (-\frac{3}{4})(\frac{4}{5}) = -\frac{3}{5}$ . Thus, the terminal point determined by  $t$  is  $P(\frac{4}{5}, -\frac{3}{5})$ , and so  $\sin t = -\frac{3}{5}$ ,  $\cos t = \frac{4}{5}$ ,  $\csc t = -\frac{5}{3}$ ,  $\sec t = \frac{5}{4}$ ,  $\cot t = -\frac{4}{3}$ .
63.  $\sec t = 2$  and  $\sin t < 0$ , so  $t$  is in quadrant IV. Thus,  $\cos t = \frac{1}{2}$  and the terminal point determined by  $t$  is  $P(\frac{1}{2}, y)$ . Since  $P$  is on the unit circle  $(\frac{1}{2})^2 + y^2 = 1$ . Solving for  $y$  gives  $y = \pm\sqrt{1 - \frac{1}{4}} = \pm\sqrt{\frac{3}{4}} = \pm\frac{\sqrt{3}}{2}$ . Since  $t$  is in quadrant IV,  $y = -\frac{\sqrt{3}}{2}$ . Thus the terminal point is  $P(\frac{1}{2}, -\frac{\sqrt{3}}{2})$ , and so  $\sin t = -\frac{\sqrt{3}}{2}$ ,  $\cos t = \frac{1}{2}$ ,  $\tan t = -\sqrt{3}$ ,  $\csc t = -\frac{2}{\sqrt{3}} = -\frac{2\sqrt{3}}{3}$ ,  $\cot t = -\frac{1}{\sqrt{3}} = -\frac{\sqrt{3}}{3}$ .
65.  $\sin t = -\frac{1}{4}$ ,  $\sec t < 0$ , so  $t$  is in quadrant III. So the terminal point determined by  $t$  is  $P(x, -\frac{1}{4})$ . Since  $P$  is on the unit circle  $x^2 + (-\frac{1}{4})^2 = 1$ . Solving for  $x$  gives  $x = \pm\sqrt{1 - \frac{1}{16}} = \pm\sqrt{\frac{15}{16}} = \pm\frac{\sqrt{15}}{4}$ . Since  $t$  is in quadrant III,  $x = -\frac{\sqrt{15}}{4}$ . Thus, the terminal point determined by  $t$  is  $P(-\frac{\sqrt{15}}{4}, -\frac{1}{4})$ , and so  $\cos t = -\frac{\sqrt{15}}{4}$ ,  $\tan t = \frac{1}{\sqrt{15}} = \frac{\sqrt{15}}{15}$ ,  $\csc t = -4$ ,  $\sec t = -\frac{4}{\sqrt{15}} = -\frac{4\sqrt{15}}{15}$ ,  $\cot t = \sqrt{15}$ .