

$$66. \frac{\cos \theta}{1 - \sin \theta} = \frac{\cos \theta}{1 - \sin \theta} \cdot \frac{1 + \sin \theta}{1 + \sin \theta} = \frac{\cos \theta(1 + \sin \theta)}{1 - \sin^2 \theta} = \frac{\cos \theta(1 + \sin \theta)}{\cos^2 \theta} = \frac{1}{\cos \theta} + \frac{\sin \theta}{\cos \theta}$$

$$= \sec \theta + \tan \theta$$

$$68. \frac{1 + \tan x}{1 - \tan x} = \frac{1 + \frac{\sin x}{\cos x}}{1 - \frac{\sin x}{\cos x}} \cdot \frac{\cos x}{\cos x} = \frac{\cos x + \sin x}{\cos x - \sin x}$$

$$70. \frac{1}{1 - \sin x} - \frac{1}{1 + \sin x} = \frac{(1 + \sin x) - (1 - \sin x)}{(1 - \sin x)(1 + \sin x)} = \frac{2\sin x}{1 - \sin^2 x} = \frac{2\sin x}{\cos^2 x} = 2 \frac{\sin x}{\cos x} \cdot \frac{1}{\cos x}$$

$$= 2 \tan x \sec x$$

$$72. \frac{1 + \sin x}{1 - \sin x} - \frac{1 - \sin x}{1 + \sin x} = \frac{(1 + \sin x)^2 - (1 - \sin x)^2}{(1 - \sin x)(1 + \sin x)} = \frac{1 + 2\sin x + \sin^2 x - 1 + 2\sin x - \sin^2 x}{1 - \sin^2 x}$$

$$= \frac{4\sin x}{\cos^2 x} = 4 \frac{\sin x}{\cos x} \cdot \frac{1}{\cos x} = 4 \tan x \sec x$$

$$74. \tan^2 x - \cot^2 x = (\sec^2 x - 1) - (\csc^2 x - 1) = \sec^2 x - \csc^2 x$$

$$76. \frac{\cot x + 1}{\cot x - 1} = \frac{\cot x + 1}{\cot x - 1} \cdot \frac{\tan x}{\tan x} = \frac{\tan x \cot x + \tan x}{\tan x \cot x - \tan x} = \frac{1 + \tan x}{1 - \tan x}$$

$$78. \frac{\tan v - \cot v}{\tan^2 v - \cot^2 v} = \frac{\tan v - \cot v}{(\tan v - \cot v)(\tan v + \cot v)} = \frac{1}{\tan v + \cot v} = \frac{1}{\frac{\sin v}{\cos v} + \frac{\cos v}{\sin v}} \cdot \frac{\sin v \cos v}{\sin v \cos v}$$

$$= \frac{\sin v \cos v}{\sin^2 v + \cos^2 v} = \sin v \cos v$$

$$80. \frac{\tan x + \tan y}{\cot x + \cot y} = \frac{\frac{\sin x}{\cos x} + \frac{\sin y}{\cos y}}{\frac{\cos x}{\sin x} + \frac{\cos y}{\sin y}} = \frac{\frac{\sin x \cos y + \cos x \sin y}{\cos x \cos y}}{\frac{\cos x \sin y + \sin x \cos y}{\sin x \sin y}}$$

$$= \left(\frac{\sin x \cos y + \cos x \sin y}{\cos x \cos y} \right) \left(\frac{\sin x \sin y}{\cos x \sin y + \sin x \cos y} \right) = \frac{\sin x \sin y}{\cos x \cos y} = \tan x \tan y$$